

Unit 16

Day 5

Evaluating Logarithms

Section 5.4

COMMON LOGARITHMS

The bases 10 and e are so important for logarithms that scientific and graphing calculators have keys for these bases.

For now on, we will abbreviate $\log_{10} x$ as $\log x$.

natural log $\ln x$

CHANGE-OF-BASE THEOREM

For any positive real numbers x , a , and b , where
 $a \neq 1$ and $b \neq 1$:

$$\log_a x = \frac{\log_b x}{\log_b a}$$

Use the change-of-base theorem to find an approximation for each of the following logarithms. Give the answer to four decimal places.

$$\begin{aligned} 1) \quad \log_6 3 &= \frac{\log 3}{\log 6} \\ &= \frac{.4771}{.7782} \\ &= .6131 \end{aligned}$$

$$\begin{aligned} 2) \quad \log_2 5 &= \frac{\log 5}{\log 2} \\ &= 2.3219 \end{aligned}$$

3)

$$\log_7 28$$

$$\frac{\log 28}{\log 7} = 1.7124$$

4)

$$\log_5 180$$

$$\frac{\log 180}{\log 5} = 3.2266$$

4)

$$\log_3 142$$

$$\frac{\log 142}{\log 3} =$$

~~$$1.7124$$~~

$$4.5110$$

5)

$$\log_{16} 27$$

~~$$3.2266$$~~

$$1.1887$$

HOMEWORK

Day 5 p. 392: 35-42

Review p 416: 9-32, 39-42, 54-58